

# Analysis of $K_s^0 K_s^0$ and $\pi^+ \pi^- \pi^0$ final states in two photon collisions at LEP

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**Abstract.** The  $K_s^0 K_s^0$  and  $\pi^+ \pi^- \pi^0$  final states in two-photon collisions are studied with the L3 detector at LEP. A full energy dependent partial wave analysis demonstrates that the two-photon mass spectra are dominated by the formation of tensor mesons. Their masses, widths and two-photon partial widths are determined.

## 1 Introduction

An important step in the development of a nonperturbative approach in QCD at low and intermediate energies is an identification and classification of the strongly interacting particles - hadrons. An important tool for the investigation of hadronic states is provided by two-photon interactions.

Exclusive states are produced in two-photon collisions in clean conditions and with restricted quantum numbers. In the reaction

$$e^+ e^- \rightarrow e^+ e^- \gamma \gamma \rightarrow e^+ e^- R$$

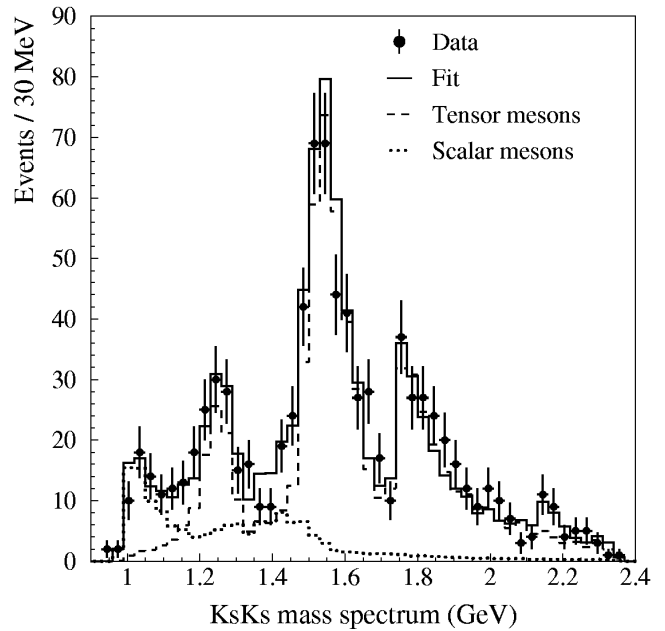
$R$  denotes a neutral unflavoured meson with positive charge conjugation parity  $C = +1$ . Events, studied in this work, have small 4-momentum transferred squared ( $Q^2 \approx 0$ ), the photons are quasi-real, odd spin states are forbidden. For  $\gamma\gamma \rightarrow K_s^0 K_s^0$  allowed states are  $J^{PC} = 0^{++}, 2^{++}, 4^{++}, \dots (2n)^{++}$ . In  $\gamma\gamma \rightarrow \pi^+ \pi^- \pi^0$  the  $0^+$  state is excluded by parity conservation, so that only isovector  $q\bar{q}$  states can be produced ( $I^G = 1^-$ ). Allowed states are  $J^{PC} = 0^{-+}, 2^{++}, 2^{-+}, \dots$ .

The reactions are investigated with the L3 detector [1] at LEP in untagged two-photon events (final state electron and positron are not detected). Data are analysed with full energy dependent Partial Wave Analysis (PWA), based on the approach of [2,3,4]. In case of the  $K_s^0 K_s^0$  channel an analysis is also done based on the SU(3) nonet classification, and SU(3) relations are imposed on parameters.

## 2 $\gamma\gamma \rightarrow K_s^0 K_s^0$

The  $K_s^0 K_s^0$  final state is analysed at center of mass energies from 91 to 209 GeV and with total integrated luminosity

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**Fig. 1.**  $K_s^0 K_s^0$  mass distribution. Continuous histogram - fit of data with SU(3) relations imposed

$L=806 \text{ pb}^{-1}$  (LEPI:  $\sqrt{s}=91 \text{ GeV}$ ,  $L=143 \text{ pb}^{-1}$ ; LEP II:  $\sqrt{s}=183\text{-}209 \text{ GeV}$ ,  $L=663 \text{ pb}^{-1}$ ).

Events with four charged tracks (two positive and two negative) are selected. Two opposite-pairs form secondary vertices with “invariant” distance from nominal interaction point  $d_0 = d \cdot \frac{M_{K_s^0}}{P_{K_s^0}} > 1.5 \text{ mm}$ . To select kaon pairs, masses of two  $K_s^0$  candidates,  $m_{+-}$ , are required to be inside a circle of 40 MeV radius around the central  $K_s^0$  mass value indicating  $K_s^0 K_s^0$  production. The total transverse momentum of all tracks  $P_t = |\sum \mathbf{p}_t|$  has to be less than 0.3 GeV (to select an exclusive state). 870 events are selected.

**Table 1.** Parameters obtained from SU(3) based fit of  $K_s^0 K_s^0$  state

	First nonet			Second nonet		
	$a_2(1320)$	$f_2(1270)$	$f_2'(1525)$	$a_2(1700)$	$f_2(1560)$	$f_2(1750)$
Mass (MeV)	$1304 \pm 10$	$1277 \pm 6$	$1523 \pm 5$	1730*	1570*	$1755 \pm 10$
Width (MeV)	$120 \pm 15$	$195 \pm 15$	$104 \pm 10$	340*	160*	$67 \pm 12$
$K\bar{K}$ width (MeV)	$7.0_{-1.5}^{+2.0}$	$7.5 \pm 2$	68*	$5 \pm 3$	$2 \pm 1$	$23 \pm 7$
Radius (fm)	0.55*	0.55*	0.5*	0.55*	0.55*	0.5*
Nonet coupling (MeV)	$0.8 \pm 0.1$	$0.9 \pm 0.1$	$1.05 \pm 0.1$	$0.38 \pm 0.05$		
Mixing angle (degrees)	-1 $\pm$ 3			$-10_{-10}^{+5}$		
$\gamma\gamma$ width (KeV)	0.91*	$2.55 \pm 0.15$	$0.13 \pm 0.03$	0.18*	$0.5 \pm 0.1$	$0.11 \pm 0.04$
$\pi\pi$ width (MeV)		$148 \pm 8$	$0.2_{-0.2}^{+1.0}$		30*	$1.3 \pm 1.0$
$\pi\eta$ width (MeV)	$18.5 \pm 3$			$9.5 \pm 2$		
$\eta\eta$ width (MeV)		$1.8 \pm 0.4$	$5.0 \pm 0.8$		$1.2 \pm 0.3$	$2.0 \pm 0.5$

\* fixed from other data

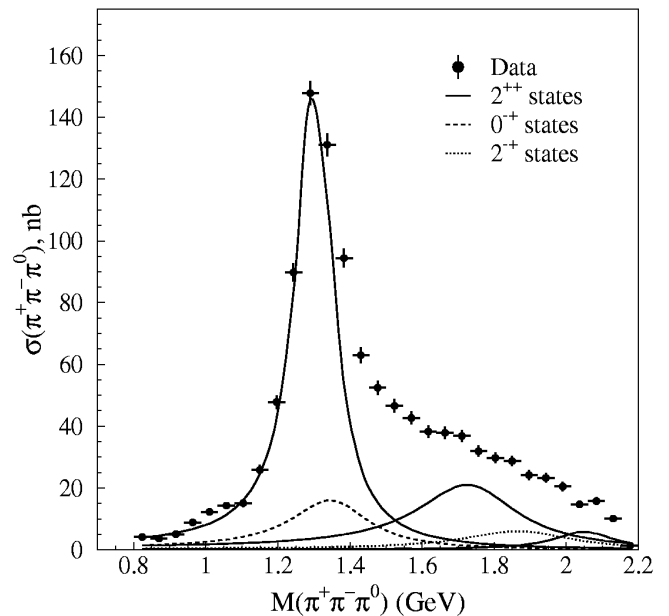
Figure 1 presents the mass distribution of selected  $K_s^0 K_s^0$  pairs (points), which shows rich resonance structure. The main contribution comes from tensor mesons. Resonances of the first tensor nonet are:  $a_2(1320)$  and  $f_2(1270)$  (a small signal due to a destructive interference) and  $f_2'(1525)$ , which dominates the spectrum. A signal from  $a_0(980)$  is clearly seen near process threshold. Parameters of the scalar amplitudes ( $a_0$  and  $f_0$ ) are fixed (see [5],[6]). Angular distributions show that the 2150 MeV peak is most likely a  $4^{++}$  state. The peak at 1700-1800 MeV (observed in a previous L3 analysis of the  $K_s^0 K_s^0$  channel [7,8]) is well described by a tensor meson  $f_2(1750)$ . At the same time a dip is well reproduced between  $f_2'(1525)$  and  $f_2(1750)$  due to destructive interference of these states. If, instead, a scalar meson  $f_0(1710)$  is introduced, the fit fails to reproduce both the dip and a slope above 1800 MeV. The  $f_2(1560)$  and  $a_2(1700)$  practically do not contribute to the cross section. Their parameters are fixed, respectively, from Crystal Barrel data [9, 10] and from the L3 analysis of  $\pi^+ \pi^- \pi^0$  state (see below).

A fit using SU(3) relations gives a very good description of the data (parameters obtained are shown in Table 1). A description of data in the nonet approach has a significant problem if the peak at 1750 MeV is assumed to be a scalar state. On the contrary as a tensor state it fits well into a second tensor nonet together with  $f_2(1560)$  and  $a_2(1700)$ . The parameters, obtained here for  $f_2(1750)$ , are consistent with the previous L3 measurement [8].

As is seen from Table 1, the masses of the isoscalar tensor states are systematically lower than those of isovector states. This can be an indication of a tensor glueball in mass region 1800-2000 MeV.

### 3 $\gamma\gamma \rightarrow \pi^+ \pi^- \pi^0$

$\pi^+ \pi^- \pi^0$  final state is analysed at LEP II energies  $\sqrt{s}=183$  - 209 GeV,  $L=609 \text{ pb}^{-1}$ . Events have two tracks of opposite charge, originating from the interaction point, two isolated electromagnetic clusters, forming a  $\pi^0$  ( $0.065 <$



**Fig. 2.** Mass distribution of three pions and contribution of different states into cross section

$m_{\gamma\gamma} < 0.220$  GeV), and total transverse momentum  $P_t = |\sum \mathbf{p}_t| < 0.1$  GeV. About 18 thousand events are selected.

The mass distribution for three pions is shown in Fig. 2. Possible states are  $2^{++}$ :  $a_2(1320)$ ,  $a_2(1700)$ ,  $a_2(2030)$ ;  $2^{-+}$ :  $\pi_2(1670)$ ;  $0^{-+}$ :  $\pi(1300)$ . The distribution is clearly dominated by production of the  $a_2(1320)$  state. There is also a pronounced shoulder at masses higher than 1500 MeV. PWA is done in the mass range  $1.1 < M(\pi^+ \pi^- \pi^0) < 2.2$  GeV.

The model, used for PWA, supposes a cascade decay

$$\gamma\gamma \rightarrow R \rightarrow \pi R', \quad R' \rightarrow \pi\pi.$$

In the  $\pi^\pm \pi^0$  mass spectrum  $\rho(770)$  dominates, and  $\rho(1450)$  is also seen. In the  $\pi^+ \pi^-$  system only  $f$ -states ( $J^{PC} = 0^{++}, 2^{++}, \dots$ ) are possible.  $f_0(980)$  and  $f_0(1500)$  give very

**Table 2.** Mass, width and the product of  $\Gamma_{\gamma\gamma}$  times  $\text{Br}(3\pi)$  for observed resonances

Resonance	M (MeV)	$\Gamma(\text{MeV})$	$\Gamma_{\gamma\gamma}\text{Br}(3\pi)$ (KeV)
$a_2(1320)$	$1302 \pm 3 \pm 6$	$118 \pm 6 \pm 10$	$0.65 \pm 0.05$
$a_2(1700)$	$1725 \pm 25 \pm 10$	$340 \pm 40$	$0.37^{+0.12}_{-0.08}$
from [12]	$1752 \pm 21 \pm 4$	$150 \pm 115$	$0.29 \pm 0.04$
$a_2(2030)^*$	$2030 \pm 20$	$205 \pm 25$	$0.11 \pm 0.04$
$\pi(1300)$	$1350 \pm 40$	$320 \pm 50$	$\leq 0.8$
$2^{-+}$	$1870 \pm 60$	$325 \pm 40$	$0.15 \pm 0.03$
$\pi_2(1670)^*$	1670	260	$\leq 0.1$

\* fixed from other data

small contributions and they are omitted.  $f_2(1270)$  produces some signal. A  $\pi\pi \rightarrow \pi\pi$  S-wave amplitude (from  $\pi\pi$  threshold up to 2 GeV) was required. Background is described by a second order polynomial function depending on the  $3\pi$  mass squared.

To reproduce the data ( $3\pi$  mass,  $2\pi$  masses and all angular distributions) three tensor states are needed  $a_2(1320)$ ,  $a_2(1700)$  and  $a_2(2030)$ , a scalar, which can be identified as  $\pi(1300)$ , and a  $2^{-+}$  state at high  $3\pi$  masses. Masses and widths for resonances are listed in Table 2.

Tensor mesons are mainly produced from  $^5S_2$  two-photon initial state. For  $a_2(1320)$  the ratio with the  $^1D_2$  wave is found to be:

$$\frac{\sigma(\gamma\gamma(^5S_2) \rightarrow a_2(1320))}{\sigma(\gamma\gamma(^1D_2) \rightarrow a_2(1320))} = 8.2 \pm 0.6$$

The corresponding value for the  $a_2(1700)$  is  $2.5 \pm 1.0$ . The corresponding ratio of couplings is  $0.60 \pm 0.20$ , in good agreement with expectation [11]  $0.54 \pm 0.16$  for the first recurrence of the  $a_2(1320)$ . The  $a_2(1700)$  state was first observed in the previous L3 analysis [12] of  $\pi^+ \pi^- \pi^0$  with limited statistics. This state is confirmed by the present full energy analysis, and its parameters are consistent with the previous measurement (see Table 2). The  $a_2(1700)$  has a significant branching fraction into  $f_2(1270)\pi$ :

$$\frac{\text{Br}(a_2(1700) \rightarrow \rho(770)\pi)}{\text{Br}(a_2(1700) \rightarrow f_2(1270)\pi)} = 3.4 \pm 0.4$$

At higher  $3\pi$  mass values a contribution from another isovector tensor state,  $a_2(2030)$ , is needed. The mass and width of this resonance can not be determined from present analysis, and they are fixed to values given in [13]. The  $\pi(1300)$  state, when introduced in the analysis, appreciably improves the likelihood. But this state produces a uniform angular distribution and is similar to background, so only an upper limit is estimated for the  $\gamma\gamma$  width of this state. A  $2^{-+}$  signal is found at masses higher than  $\pi_2(1670)$ . If a mass of  $2^{-+}$  is left free, it always moves to 1850-1900 mass region, giving indication of new  $2^{-+}$  state

(see Table 2). For  $\pi_2(1670)$  an upper limit on the  $\gamma\gamma$  width is defined (parameters of  $\pi_2(1670)$  are fixed from [14]).

## 4 Conclusions

For  $\gamma\gamma \rightarrow K_s^0 K_s^0$ :

- PWA favors a description of the peak at 1750 MeV by a tensor state  $f_2(1750)$ .
- If nonet relations are applied this state fits naturally into a second tensor nonet together with  $f_2(1560)$  and  $a_2(1700)$  states.
- The data define very well the mixing angles for two tensor nonets:  $(-1^\circ \pm 3^\circ)$  for the first and  $(-10^{+5^\circ}_{-10^\circ})$  for the second.
- There is an indication for a  $4^{++}$  state:  $M=(2150 \pm 30)$  MeV,  $\Gamma=(50 \pm 20)$  MeV.

For  $\gamma\gamma \rightarrow \pi^+ \pi^- \pi^0$ :

- The characteristics of the dominant  $a_2(1320)$  state are found. The measured mass is lower than the world average [14] since in the present fit it is the amplitude pole and not the central value of the mass spectrum.
- A strong signal is observed from the first radial excitation isovector tensor state  $a_2(1700)$ :  $M = 1725 \pm 25 \pm 10$  MeV,  $\Gamma = 340 \pm 40$  MeV.
- Another isovector state with the mass 2030 MeV is found to be significant.
- There is also a signal from  $\pi(1300)$  and an indication for a  $2^{-+}$  signal in the region of 1870 MeV.

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